Roundness Estimation of Sedimentary Rocks Using Eliptic Fourier and Deep Neural Networks

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Abstract—**Sedimentary rocks analysis is useful in geological science, economic sector, and risk evaluation. Roundness is a morphological parameter that provide information to characterize and classify sedimentary material. Roundness degrees is estimated from the contour of the particle. Waddell (1932) proposed a remarkable method based on the measurement of particle's curvature. This method is accurate; nevertheless, it is not invariant to scale and rotation. This problem can be solved by mapping the contour to the frequency-domain, however, spectral analysis is a difficult task. Based on these two approaches, we propose to use a deep neural network whose input is the elliptical Fourier spectrum and target is roundness proposed by Wadell. The training database consists of 623 real-rocks images from some geological phenomena. We have found the neural networks perform very well on the 88.8% of rocks.**

I. Introduction

Sedimentary rocks are the most abundant in the Earth's crust, covering around 80%. Their study is key to understanding the geological processes that have occurred on earth. Sedimentary rocks are very important in the economy field because they are related to oil, natural gas, coal, salt, sulfur, potassium, gypsum, limestone, phosphate, uranium, among other minerals [1]. Furthermore, in some cases, they represent a risk for populations settled near volcanoes or large sediments [2].

Sedimentary rocks are characterized by their physical, chemical, and mineralogical composition. Physical characteristics are described by three parameters; size, morphology, and fabric (orientation). Accurate measurement of these parameters enables inferences about the origin, transport processes, rheological and climatic environment, and the deposition of the sediment. Size and fabric have been extensively studied and there are well-established techniques for measuring them [3]. On the other hand, morphology is a recent concept, in comparison to the others and is still in development and search for universal concepts [4]. Morphology describes the shape of rocks using contour measurements. Morphology of rocks by three parameters: form, roundness, and surface texture (roughness). Morphology of rocks consists of three parameters: form, roundness, and surface texture (roughness). These three parameters are hierarchical and of different scales, so one does not affect the other. Form is the highest-hierarchy feature that is related to the general appearance of the rock. Roundness is an intermediate-hierarchy feature superimposed on form. The degree of roundness or angularity is related to the curves and the main corners of the contour. Roughness or surface texture refers to finer irregularities overlapping on form and roundness [5]. These parameters are illustrated in hierarchical order in Fig. 1.
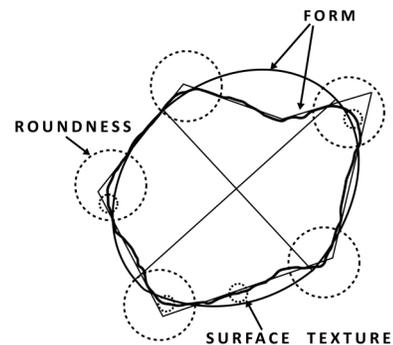
Fig. 1. Hierarchical order proposed by Barret. Features corresponding to irregularities of form, roundness, and surface texture.

Form describes the general appearance of the rock, it is a coarse sketch of contour. There are some expressions to measure form, the most used, in the geological field, is the proposed by Wadell [6] which is obtained from the relationship between the radius of the circle whose area is equal to the particle and the radius of the smallest circle that inscribes the particle. Form is a well-established concept. On the other hand, roundness is a complex concept that is difficult to estimate. For this reason, we dedicate

the present work to this parameter. To measure the degree of roundness, there are two approaches; those based on curvature [7] and those using frequency analysis [8]. The curvature-based method defines the degree of roundness as the ratio of the mean radius of curvature of the corners of a particle to the radius of the largest circumscribed circle possible. This method is simple and accurate, however it is a scale dependent method. The Fourier-based methods are invariant to scale, rotation and translation, however analyzing the spectrum is a complicated issue and of high computational cost [8].

In this work, we propose to use neural networks to estimate the roundness of sedimentary rocks. The input variable to the neural network are the range from 3 to 40 of coefficients a,b,c and d of the elliptical Fourier spectrum. The Fourier spectrum was chosen as the input variable because it is invariant to scale, rotation, and translation. The degree of roundness, calculated with the curvature method proposed by Wadell [6], was used as the objective of the neural network. To calculate the roundness, we use the algorithm developed by Zheng and Hryciw [7]. The proposed neural network has the following architecture: 6-layer neural network, the input layer with 148 neurons, the same size as the input, and Sigmoid activation function; 4 hidden layers with several different quantities of neurons each, the next layer always have less neurons than the last one, with Sigmoid activation function; and the output layer with a single neuron and Sigmoid activation function. The database to train the neural network contains 623 real-rocks images from some geological phenomena. The neural network model has a mean squared error of $5E-3$ and a mean error of $1E-2$. The neural network enables much faster processing. The roundness is estimated at 2800 times faster than the algorithm developed by Zheng and Hryciw. In addition, the method proposed is invariant to scale, rotation, and translation. Using a neural network we have combined the potentialities of the method based on curvature and frequency analysis.

II. Materials and Methods

In this section, we explain the concepts and mathematical expressions to estimate the roundness. The input variable to the neural network, elliptical Fourier, is described too.

A. Roundness

Roundness is a textural characteristic resulting from various geological processes. Roundness is strongly defined during transport and deposition of sediments. Collisions, abrasion, friction, comminution, exposure time, and pathway are the main processes that determine the roundness of a particle. The detailed analysis enables inferences about the type of kinetic and mechanical interaction interparticle [9]. Roundness can help discriminate between reworked and primary deposits, a common problem in sedimentology. Briefly, the roundness study enables determines the set of environmental conditions of each sediment [10].

Roundness is a second-order property which is independent of the form and surface texture. The roundness of a rcok is related to the smoothness (or angularity) of particles. These variations are expressed in corners and edges. The roundness of a partile can be estimated by two approaches: curvature and frequency contour analysis. Frequency analysis is described in section elliptical Fourier. The curvature approach was proposed Wadell [6]. The curvature approach consists of finding the most significant curvatures in the contour. These curvatures are associated with the angularity of the particle. The smaller radius of curvature, the greater corner angle. The more significant curvatures there are, the more angular the contour will be. An example is shown in Fig. 2.
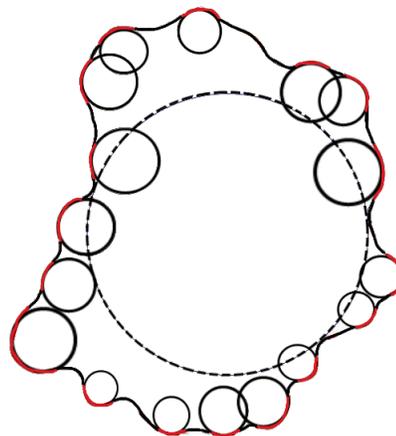
Fig. 2. Illustration of the method, proposed by Wadell, to measure the degree of roundness. The circle dotted line corresponds to maximum inscribed circle and the circles solid line correspond to main corners.

The maximum inscribed circle is used to normalize. This fact is important because the maximum circumscribed circle can be used to normalize. Thus the degree of roundness of a corner can be expressed as r_n/R, where r_n is the radius of curvature of the corner n and R is the radius of the maximum circumscribed circle. Wadell [6] expressed the total roundness of a particle as

$$D_g = \sum_{n=0}^{N-1} \frac{r_n}{R}, \tag{1}$$

where N is the number of total corners in the contour. In this way, the range of roundness is between 0 and 1, being 0 a contour without corners (perfect circle) and 1 a contour with the possible maximum number of corners. The algorithm works properly, however, the threshold to identify between corners and non-corners depends on the scale. An inappropriate value, for this threshold, can lead to a considerable error.

B. Elliptic Fourier

Frequency analysis consists in obtaining the Fourier transform of the contour. In frequency, the three morphological characteristics are divided into frequency ranges. The low-frequency range is related to form, the medium-frequency range to roundness, and the high-frequency to roughness [8]. However, determining the limits of different morphological orders is not an easy task. It has been an unsolvable problem since the method was first proposed. To date, these limits are obtained empirically, with high uncertainty.

Because the particle contour is closed, elliptical Fourier is used. The elliptical Fourier method was proposed by Kuhl [11] which consists in obtaining the Fourier coefficients directly from the chain code of the contour. The chain code approximates the contour by a sequence of lines consisting of eight directions, Fig. 3.
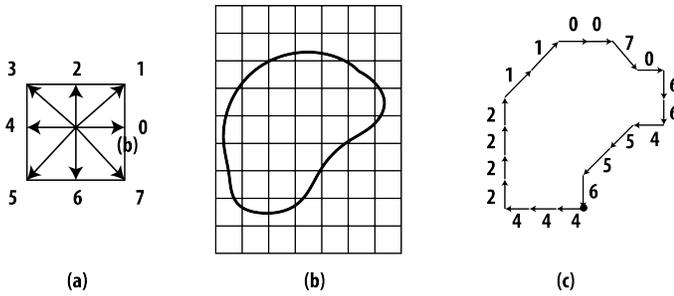
Fig. 3. Chain code. (a) Directions, (b) closed contour y (c) chain elements. The dot indicates the chain start whose result is 4442222110070664556.

Chain code can be expressed in two coordinates; x y y axis, so the elements x and y of the chain are independent. The expressions for the Fourier coefficients of the component x are

$$a_n = \frac{T}{2n^2\pi^2} \sum_{p=1}^{K} \frac{\Delta x_p}{\Delta t_p} [\cos \frac{2n\pi t_p}{T} - \cos \frac{2n\pi t_{p-1}}{T}], \quad (2)$$

$$b_n = \frac{T}{2n^2\pi^2} \sum_{p=1}^{K} \frac{\Delta x_p}{\Delta t_p} [\sin \frac{2n\pi t_p}{T} - \sin \frac{2n\pi t_{p-1}}{T}], \quad (3)$$

where, K is the number of pixels of contour, T the fundamental period, Δx_p incremental change on the x axis, Δt_p time incremental change. In a similar way, the coefficients of the component y are calculated by the following expressions

$$c_n = \frac{T}{2n^2\pi^2} \sum_{p=1}^{K} \frac{\Delta y_p}{\Delta t_p} [\cos \frac{2n\pi t_p}{T} - \cos \frac{2n\pi t_{p-1}}{T}], \quad (4)$$

$$d_n = \frac{T}{2n^2\pi^2} \sum_{p=1}^{K} \frac{\Delta y_p}{\Delta t_p} [\sin \frac{2n\pi t_p}{T} - \sin \frac{2n\pi t_{p-1}}{T}], \quad (5)$$

These four series of coefficients can be expressed by circular phasors, one for each axis; however, they can be drawn by a single elliptical phasor, hence its name. The invariance to scale, rotation, and translation are reached by normalization and rotation of angle of the first ellipse to zero, the expressions to achieve this can be consulted in [11]. The elliptical Fourier is two dependent spectra. Dependence complicates the delimitation of frequency ranges corresponding to form and roundness.

C. Using deep neural networks to determine form and roundness

A neural network is a type of machine learning which simulates the human learning mechanism. The neuron is the basic unit. A neural network contains a large number of neurons connected to each other. The connection between the neurons is known as synapse and its strength is determined by an external stimulus. In the artificial and biological neural network, the change in synaptic weight enables learning. The stimulus in artificial neural networks is provided by the training data containing input-output pairs of the function to be learned [12]. Neuron should be activated or not depending on whether it is relevant to the prediction. The function that performs this process is known as the activation function. The neural network is organized in layers. A layer consists of several neurons and has a specific order in relation to the others. The first layer receives the input data, the last layer provides the result. The intermediate layers are called hidden layers [13].
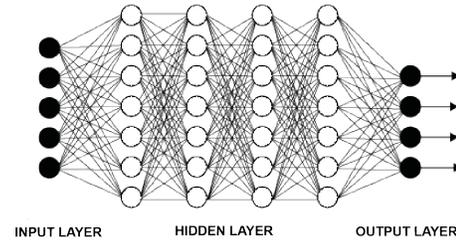
Fig. 4. Typical structure neural network.

A deep neural network consists of calculations carried out by many layers. Fig. 4 shows a deep neural network architecture with 4 hidden layers. The nodes of a layer are connected to the nodes of the previous and next layer. These types of networks are used to adjust complex models that requires a more sophisticated estimation [14].

To link curvatures and frequency approaches, we proposed using deep neural networks to estimate the roundness of sedimentary rocks. The input variable to the neural network are the range from 3 to 40 of coefficients a,b,c and d of the elliptical Fourier spectrum. We chose the spectrum as the input variable because it is invariant to scale, rotation, and translation. The degree of roundness obtained by the radius of the curvature (method described above) is used as the target value.

To explain the methodology used, Fig. 5 sketches the flow diagram of the proposed method.
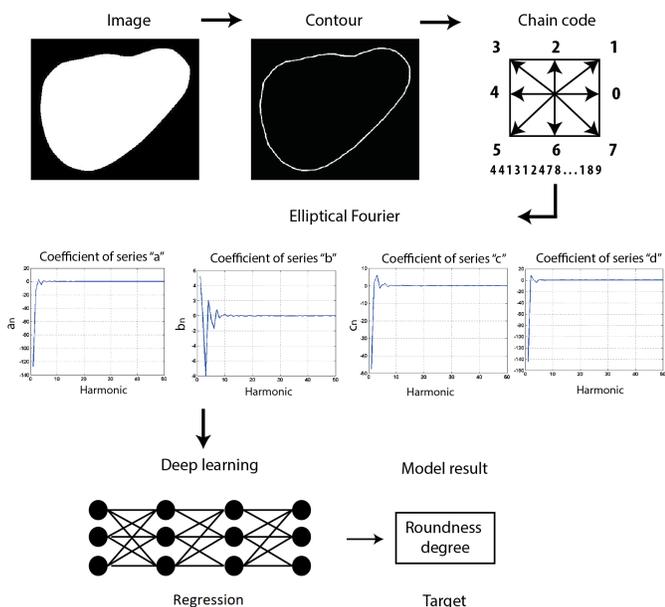
Fig. 5. Flow-chart of the developed method to measure the roundness of sedimentary rocks

The database to train and test the deep neural network was built from 623 images of real rocks. The rocks analyzed correspond to pyroclastic falls, block and ash flow, debris avalanche and lahars. The database is available at https://github.com/Gamalielmch/DNN_roundness.

The architecture used for the neural network is: 6-layer neural network, the input layer with 148 neurons, the same size as the input, and Sigmoid activation function; 4 hidden layers with several different quantities of neurons each, the next layer always have less neurons than the last one, with Sigmoid activation function; and the output layer with a single neuron and Sigmoid activation function.

III. RESULTS AND DISCUSSION

Results of analysis reveal that the deep neural network with 6 layers, single input and output layer and twenty seven hidden layers, is the most appropriate architecture to measure roundness dregree.

The Sigmoid activation function was chosen for all layers because the range of our output is in between 0 and 1, so, even if the Sigmoid suffers with the vanishing gradient problem, it is perfect because the outputs are defined when the gradient is more than 0, then, the error can be propagated properly among the network. Deep neural network training was performed in Python v3.7.3 using the Jupyter Notebook v5.7.8 platform, using the keras and sklearn libraries [15]. The result of the training is shown in Fig. 6.

As can be seen from Fig. 6, almost all model predictions simulate the roundness degree properly. The deep neural network has a mean squared error (MSE) of $5E-3$ and
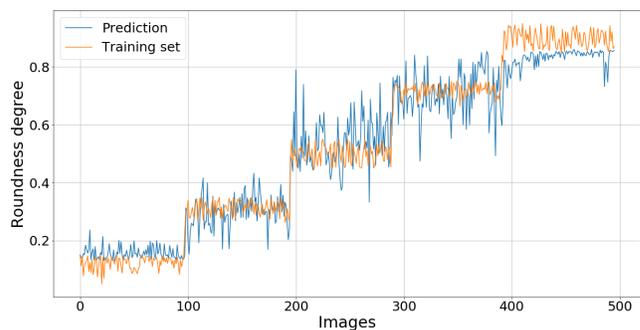
Fig. 6. Result of deep neural network training

a mean error of $1E-2$. For more detail, the histogram of absolute difference is shown in Fig. 7. The 82% shows a difference of less than 0.1 and 51 % of less than 0.05.
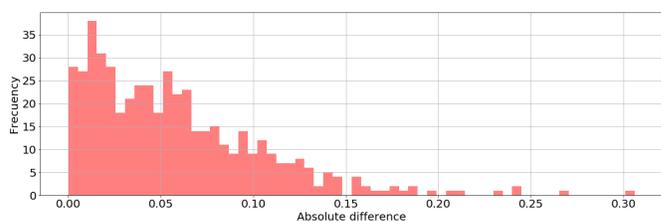
Fig. 7. Absolute differences Histogram of the training set. Difference between the predicted value by the neural network and the roundness measured by the Zheng and Hryciw algorithm

To test the deep neural network we have reserved a set of 125 images from the database which were chosen randomly. Fig. 9 shows the results of estimation for test set. The MSE is 0.01 and mean error is 0.023.
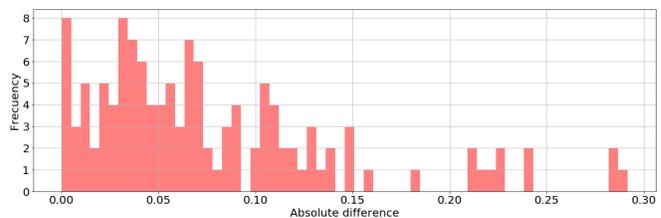
Fig. 8. Absolute differences Histogram of the test set.

The fitting of the deep neural network is accurate for 82% of cases, since a difference of less than 0.1 is very acceptable in geological studies. Furthermore, Fig. 8 shows the 70% of the images below of 0.1 and 88.8% below of 0.15. This difference is acceptable considering that in geology rocks are classified into 5 classes. These five classes have a range of 0.2.

IV. CONCLUSIONS

This work describes the implementation of a deep neural network to estimate the roundness of sedimentary rocks. We use two approaches, curvature and frequency analysis.
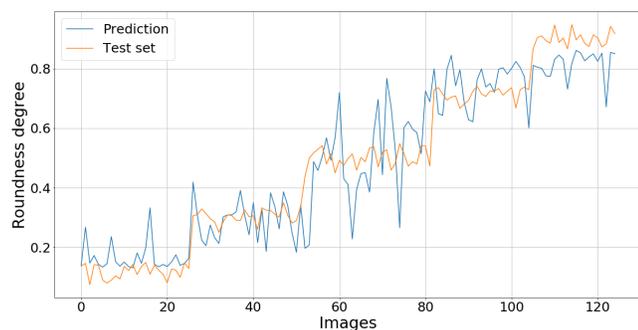
Fig. 9. Result of deep neural network for test set

The input data are the 3 to 40 coefficients of elliptical Fourier and the target data are the curvature of the main corners of the contour. Using these two approaches, we developed an invariant method to scale, rotation, and translation. Based on several architectures, it is concluded that the deep neural network with 6 layers, with several different quantities of neurons, is the most appropriate to prediction roundness degree.

The deep neural network was trained and tested using 623 images of real rocks from some geological phenomena. The fitting of the network shows that 82 % of the training data have a difference of less than 0.1. On the other hand, the MSE of the test data was 0.01 and the mean error was 0.023, a highly acceptable difference in the geological field. The deep neural network model, proposed in this manuscript, can be easily used by readers. The model is freely distributed and available in the repository https://github.com/Gamalielmch/DNN_roundness.

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