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ABSTRACT

Early detection is fundamental for the effective treatment of breast cancer and the screening mammography is the most common tool used by the medical community to detect early breast cancer development. Screening mammograms include images of both breasts using two standard views, and the contralateral asymmetry per view is a key feature in detecting breast cancer. However, most automated detection algorithms do not take it into account. In this research, we propose a methodology to incorporate said asymmetry information into a computer-aided diagnosis system that can accurately discern between healthy subjects and subjects at risk of having breast cancer. Furthermore, we generate features that measure not only a view-wise asymmetry, but a subject-wise one. Briefly, the methodology co-registers the left and right mammograms, extracts image characteristics, fuses them into subjectwise features, and classifies subjects. In this study, 152 subjects from two independent databases, one with analog- and one with digital mammograms, were used to validate the methodology. Areas under the receiver operating characteristic curve of 0.738 and 0.767, and diagnostic odds ratios of 23.10 and 9.00 were achieved, respectively. In addition, the proposed method has the potential to rank subjects by their probability of having breast

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cancer, aiding in the re-scheduling of the radiologists' image queue, an issue of utmost importance in developing countries.

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<u>2</u>4 1. Introduction

Breast cancer represents nearly one-third of all female cancer cases in the United States [1] and is one of the global leading causes of death among women [2]. Early detection is fundamental for the effective treatment of breast cancer, and furthermore, it has been proven to help reduce mortality rates by up to 65% [3–5]. Currently, this is done with the aid of some type of medical imaging technique, such as mammography, ultrasound, magnetic resonance imaging (MRI), positron emission tomography (PET), tomosynthesis, and thermography [3].

36 Lately, thermography has gained some attention, since it is 37 a non-invasive and non-contact imaging technique. Instead of using ionizing radiation, venous access, or other invasive 38 procedure, it uses the infrared electromagnetic radiation 39 40 emitted by the human body, which is captured by a thermographic camera and analyzed by a computer-aided 41 system. Among the studies that use thermography images to 42 43 classify between subjects with and without breast cancer, Ng and Fok [6] and Ng et al. [7] reported sensitivities of 0.689 and 44 45 0.812, and specificities of 0.400 and 0.882, respectively. The screening tomosynthesis has also gained popularity, mainly 46 47 due to the fact that it may improve the detection rate and decrease the amount of false positive cases detected [8]. 48 Houssami et al. [9] compared screen-detection measures for 49 50 single-reading of tomosynthesis against double-reading mam-51 mograms, and results showed a cancer detection rate of 8.2 vs. 52 6.3 per 1000 screens.

53 Nevertheless, globally, and specially in developed coun-54 tries, the screening mammography is still the most common 55 tool used by the medical community to detect early breast cancer development. Mammograms allow clinicians to inspect 56 57 each breast in two standard views, craniocaudal (CC) and mediolateral oblique (MLO), where tissue abnormalities such 58 as calcifications, masses, and architectural distortions associ-59 ated with the early development of breast cancer can be 60 61 visualized [3]. Furthermore, in recent years, great efforts have been made to develop computer-aided detection (CADe) and 62 diagnosis (CADx) systems to assist radiologists in interpreting 63 digital mammograms [10-13]. Namely, CADe and CADx 64 systems are being developed in order to aid specialists in 65 the detection of tissue abnormalities. However, detecting such 66 67 abnormalities represent a challenging task due to the low 68 signal-to-noise ratio of the mammograms, the heterogeneous 69 tissue content of the breasts, as well as their size and shape, 70 and the size, shape, and location of the abnormalities [14-16].

71 CADe systems have been shown to be very sensitive in 72 detecting breast abnormalities [17,18], but these systems tend 73 to have low specificities, producing a large number of false positives that yield an increased amount of unnecessary 74 75 biopsies. Moreover, current methodologies detect masses

and/or calcifications not accurately aligned with the abnormalities, misleading the radiologists [15,19,20]. Nevertheless, several researchers are currently working to enhance the performance of CADe systems. An example of this can be found in the work done by de Sampaio et al. [21], in which they aimed at detecting masses. First, they classified breasts as either dense or non-dense using an adaptive algorithm. Then, they used a micro-genetic algorithm to create a texture proximity mask with which suspicious regions were localized. Lastly, they reduced the amount of false positive regions using two different approaches, one with a density-based spatial clustering and a proximity ranking of the textures extracted from the suspicious regions, and the other with a texture analysis by the combination of phylogenetic trees, local binary patterns, and support vector machines (SVM). They produced sensitivities of 0.837 and 0.930, and a rate of 0.19 and 0.15 false positives per image, for the dense and nondense breasts, respectively. Dhungel et al. [16] also presented a CADe/CADx system for the detection of masses. Using a cascade of deep learning methods refined using Bayesian optimization, this system detected 90% of masses at a rate of 1 false positive per image.

On the other hand, CADx systems can be used by radiologists as a second opinion [2,22,23] and may help in reaching a correct interpretation of abnormal findings, thus, reducing the amount of unnecessary biopsies [10,14,19,22,24]. In this regard, the previously discussed work by Dhungel et al. [16] was able to classify masses as either malignant or benign with a sensitivity of 0.90 and a specificity of 0.7. Similarly, Raghavendra et al. [25] presented an automated classification system based on Gabor wavelets, locality sensitive discriminant analysis, and a k-nearest neighbor classifier. This system yielded a mean accuracy, sensitivity, and specificity of 0.987, 0.993, and 0.983, respectively.

But, the detection of breast abnormalities can be enhanced by comparing different images of the same subject, either from the same breast at different time points [26] or by contralateral asymmetry analyses that measure the differences between the left and right breasts at a specific time point [27,28]. Furthermore, it has been shown that the contralateral asymmetry may be a risk factor for breast cancer. Nevertheless, due to the challenges that measuring such an asymmetry implies, most of the automated detection approaches to date do not take contralateral asymmetry into account [29].

Current asymmetry detection methods are often based on simple bilateral subtraction techniques [26,30]. However, breasts are composed of highly heterogeneous and deformable tissue, resulting in an unlikely perfect match between both breasts [27]. To avoid this problem, Miller and Astley [31] proposed a technique for the detection of asymmetry using a semi-automated texture-based procedure for the segmentation of the glandular tissue, measuring the shape between

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proposed methodology in detail, Section 3 reports the results of the experiments, which are thoroughly discussed in Section 4, and final conclusions are presented in Section 5.

prediction models, instead of region-specific predictions. This

methodology was validated in two independent publicly

available data sets containing both digital and analog

This paper is organized as follows: Section 2 presents the

2. Materials and methods

An overview of the proposed methodology is shown in Fig. 1. 171 Briefly, the mammograms of each subject were first pre-172 processed and segmented in order to analyze the breast tissue 173 alone. Then, the left mammograms (CC and MLO) were 174 registered into their corresponding right mammograms using 175 a B-Spline algorithm, which aligned both images in the same 176 coordinate plane. A pixel-wise subtraction was then carried on 177 between the co-registered images, yielding a CC and an MLO 178 contralateral asymmetry image per subject. Four enhance-179 ment filters were then applied to the asymmetry images, and 180 several features were extracted from each. These view-specific 181 features were combined in order to obtain subject-specific 182 features. Finally, using robust machine learning algorithms, a 183 diagnostic model able to classify subjects was generated. 184

2.1. Image processing

2.1.1. Segmentation

The automatic segmentation of the breast tissue was based on187the estimation of the background noise. An initial segmenta-188tion mask was created by estimating the background noise in189the image and discarding all pixels below five standard190

128 views for detection of the occurrence of asymmetry, obtaining 129 an accuracy of 0.867 on a validation data set of 30 screening 130 mammogram pairs. Later, Miller and Astley [32] presented a system based on measures of shape, topology, and distribution 131 of brightness. The method was tested on 104 mammogram 132 pairs, and a classification accuracy of 0.74 was obtained. 133 Similarly, Ferrari et al. [33] developed a method using 134 135 directional filtering with Gabor wavelets at different orienta-136 tions and scales. There, asymmetry was characterized by 137 variations in oriented textural patterns. Validated in a data set of 80 subjects, they achieved a classification accuracy rate of 138 0.744%. More recently, Torrents-Barrena et al. [34] also used a 139 Gabor-based detection coupled to an SVM classification stage, 140 yielding an area under the receiver operating characteristic 141 (ROC) curve (AUC) ranging from 0.724 to 0.827. Recently Evans 142 et al. [35] demonstrated that cancer signal information is 143 present in the contralateral breast where the tumor was 144 originally diagnosed, but despite this, CADe/CADx systems do 145 not fully incorporate the contralateral/asymmetry informa-146 147 tion into their process.

148 The objective of this work was to develop a CADx 149 methodology that incorporates information from both breasts, as well as their contralateral asymmetry, in order to 150 automatically classify subjects as either healthy or in risk of 151 having breast cancer. Additionally, we aimed at ranking 152 subjects within a subset by their risk of having breast cancer, 153 a characteristic that would make this CADx system of great 154 importance in developing countries, where radiologists have 155 workloads that exceed their capabilities. This methodology, 156 based on previous efforts [36], co-registers the left and right 157 images, extracts image features, and performs a classification 158 enhanced by a robust feature selection algorithm. Moreover, 159 we propose the use of subject-wise features in order to avoid 160 side- and view-dependency and to create subject-specific 161



Fig. 1 - Overview of the proposed methodology.

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191deviations of the noise level. Then, holes were removed by192applying erosion and dilation morphological operations with a193 3×3 supporting region, as defined in:

$$S_j^i(\mathbf{x}, \mathbf{y}) = (I_j^i(\mathbf{x}, \mathbf{y}) \oplus B(\mathbf{x}, \mathbf{y})) \ominus B(\mathbf{x}, \mathbf{y}), \tag{1}$$

196where $S_j^i(x, y)$ and $I_j^i(x, y)$ represent the segmented and raw197images for the ith view, either CC or MLO, and the jth side,198either left (l) or right (r), respectively; \oplus and \ominus are the dilation199and erosion morphological operations, respectively; and B(x, y)200is a 3×3 structural element. The largest region was used as the201segmentation mask while all other high intensity regions were202removed from the images.

203 2.1.2. Registration

As previously mentioned, the breast is a highly heterogeneous 204 organ whose appearance can physiologically change signifi-205 cantly between sessions. Additional dissimilarities between 206 207 images, related to patient movement, sensor noise, different 208 radiation exposure, or variation of breast compression also 209 makes this comparison difficult. Therefore, in order to 210 efficiently compare two mammograms, an initial alignment 211 using an image registration algorithm had to be carried out. 212 We performed a free-form deformation (FFD) based on B-213 splines. B-Spline deformable registration is based on deform-214 ing an image by modifying a mesh of control points following a maximization of a similarity measure [37,26]. For 2D images, 215 216 such as the mammograms involved in this study, B-splines can be modeled by the tensor product of the 1D cubic B-splines. 217 218 A 2D non-rigid transformation can be written as: $T(r_p) = r_p + d$ 219 (r_p) , where r_p represents the x and y coordinates of the pth pixel and $d(r_i)$ the deformation it suffers. The 2D deformation was 220 modeled as $d(r_p) = \langle d^x(r_p), d^y(r_p) \rangle$ using the tensor product of β , 221 the nth-order B-splines, as follows: 222

$$d^{q}(r_{p}) = \sum_{i,j} c_{i,j}^{q} \beta\left(\frac{x}{m_{x}} - i\right) \beta\left(\frac{y}{m_{y}} - i\right)$$
(2)

where $d^q(r_p)$ represents the deformation of the *p*th pixel in the qth axis plane (x or y), $c = c_{ii}^q$ is the deformation coefficient for the qth plane, and m_q is the knot spacing in the qth direction. The deformation coefficients were estimated by maximizing the similarity metric ψ , according to: 227

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$$c_{i,j}^{q} = \underset{q}{\operatorname{argmax}} \psi \langle S_{r}^{i}(\mathbf{x}, \mathbf{y}), S_{l}^{i}(\mathbf{x}, \mathbf{y}) \rangle \tag{3}$$

For this study, a multi-resolution B-Spline pyramid approach was used [36,38]. First, the left segmented mammograms were horizontally flipped. Then, both the flipped left images (CC and MLO) and their right non-flipped counterparts were re-sampled into lower resolution images. Next, the pyramids for the multi-resolution were generated and registration was performed. The left segmented mammograms were deformed using the final parameters of the registration, where a mutual information metric [39] was used as the similarity metric ψ .

2.1.3. Contralateral asymmetry

Once the images were co-registered, and in order to enhance the differences between the breasts, a pixel-wise absolute difference was computed between each left-right pair of mammograms, resulting in asymmetry images $\Delta^{i}(x, y)$, defined as:

$$\Delta^{i}(\mathbf{x}, \mathbf{y}) = \left| R^{i}_{l \to r}(\mathbf{x}, \mathbf{y}) - S^{i}_{r}(\mathbf{x}, \mathbf{y}) \right|$$
(4)

where $R_{l \rightarrow r}^{i}(x, y)$ represents the left to right registered image for the ith view. Fig. 2 shows an example of a mammogram that was co-registered and subtracted in order to highlight the bilateral differences.

2.1.4. Enhancement filters

To study the appearance of the architectural distortions, two enhancing filters were applied to the asymmetry images, a morphological high frequency enhancement filter $M^{i}(x, y)$ designed to enhance fiber-like tissues, and a Laplacian of Gaussian filter $L^{i}(x, y)$ that enhanced high frequency patterns. Additionally, since the texture between normal and abnormal tissues is different [40], two texture maps were created. The map $\sigma^{i}(x, y)$ computed the local standard deviation of the



Fig. 2 – Bilateral differences. (a) Shows a segmented mammography of a right breast, (b) its left to right registered counterpart, and (c) a color map of the resulting asymmetry image, where left and blue indicate small and large bilateral differences, respectively.

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Fig. 3 – Enhancement filters. Color map of the (a) morphological high frequency $M^i(x, y)$, (b) Laplacian of Gaussian $L^i(x, y)$, (c) local standard deviation $\sigma^i(x, y)$, and (d) local fractal dimension $F^i(x, y)$ filters. Green and blue pixels represent low and high intensity values, respectively.

264mammography images, and the map $F^i(x, y)$ the local fractal265dimension. Image processing was implemented in C++ using266ITK libraries for image manipulation [41] following the267previous implementation presented in [36]. Image 3 shows268an example of each one of these filters.

269 2.1.5. Feature extraction

A main step in any kind of pattern recognition problem is the 270 representation of data, in this case the characterization of the 271 breast tissue and their properties [42]. There are several 272 features that may be quantified aiming to detect early signs of 273 274 cancer, following our previous efforts [36], we propose the study of 44 features that are related to either the morphology 275 of the breasts or to the information found in the signal of the 276 images. All features are described in Table 1. 277

278 2.1.6. Feature combination

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In order to go from view-specific features into subject-specific
features we propose the combination of each pair of CC and
MLO features by adding and subtracting them, as defined by:

$$\begin{aligned} f_n^+(\mathbf{k}) &= f_n(\mathbf{k}^{CC}) + f_n(\mathbf{k}^{MLO}) \\ f_n^-(\mathbf{k}) &= \left| f_n(\mathbf{k}^{CC}) - f_n(\mathbf{k}^{MLO}) \right| \end{aligned}$$
 (5)

As described in Fig. 1, 88 subject-specific features were
extracted per pair of CC and MLO images, resulting in a total of
440 features per subject.

288 2.1.7. Feature selection

In recent years, several feature selection methodologies have 289 been studied for breast cancer detection. Algorithms such as 290 LASSO, KNN, SVM and others have been widely used due to 291 their performance [43,44], but as of today, there is not a *golden* 292 293 method that outperforms any other classifier in every task. We 294 previously compared the performance of several classifiers 295 [43,44,36]. Following our findings, we propose the use of FRESA. 296 CAD. FRESA.CAD is an R package that uses a bootstrapped stage-297 wise model selection (B:SWiMS) algorithm. FRESA.CAD internally computes LASSO, KNN, B:SWIMS, B:SWIMS with bagging, and B: 298 SWIMS ensembled. Therefore, we were able to compare in a 299 300 single procedure the efficiency of the methodology in a wide

range of feature selection algorithms at the same time, with exactly the same conditions in the train and validation stages. Further details of the FRESA.CAD package can be found in http:// cran.r-project.org/web/packages/FRESA.CAD/index.html.

2.2. Data acquisition

In this research, two publicly available data sets were used: The Digital Database for Screening Mammography (DDSM) and the Breast Cancer Digital Repository (BCDR). DDSM [45] is one of the largest public mammogram databases, it has been used in over 500 research projects (up to 2016). This database has 2620 cases distributed as follows: 625 healthy subjects, 1011 benign cases, and 914 malign cases. It includes two standardized CC and MLO mammograms per subjects, and was constructed by taking film-based mammograms that were then digitized using four different scanners: DBA, HOWTEK-A, LUMISYS, and HOWTEK-D. BCDR is a fairly newer public database [46]. It is maintained by the IMED Project (Development of Algorithms for Medical Image Analysis), which was created and updated by the INEGI, FMUP-CHSJ, and CETA-CIEMAT, from 2009 to 2013. The BCDR is a 100% digital mammogram database, it has 774 subjects (723 women and 1 male), from an age range between 27 years and 92 years. The images are stored in a TIFF format at 14 bits, and the type of scanner is undisclosed.

From the above mentioned data sets, we used the Lumisys subset from the DDSM data set and the whole BCDR data set. Using this data sets we created two categories, healthy subjects and non-healthy subjects. The latter refer to those with proven cancer (i.e. masses, calcification, distortions, etc.) and benign abnormalities of any type. The data sets were adjusted to exhibit the same ratio between the healthy and non-healthy groups, yielding a total of 152 subjects. Table 2 shows the detail of the data used in this research.

2.3. Experiment design

Two experiments were performed, one for each data set.335Features were first z-normalized using a rank-based inverse336normal transformation [47]. Afterwards, correlation between337pairs of features was evaluated, and for each pair of highly338

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Table 1 – Features extracted from each asymmetry image.

Category	Feature	Definition
Shape	Surface area	$A_{R}(k) = \sum_{(x,y) \in k} a_{x,y}$
	Perimeter	$P(k) = \sum_{i \in e(k)} d(e_i, e_{i+1})$
	Compactness	$C(k) = \frac{P(k)^2}{A(k)}$
	Elongation	$E(k) = \frac{\operatorname{argmax}_{q} L_{q}}{\operatorname{argmin}_{a} L_{q}}$
	² Region centroid	$q ilde{A}_{R}(\mathbf{k}) = \langle x ilde{A}_{R}(\mathbf{k}) = rac{m_{10}}{m_{00}}, y ilde{A}_{R}(\mathbf{k}) = rac{m_{01}}{m_{00}} angle$
	³ Region scatter	$S_{R}(\textbf{k}) = \langle \frac{m_{20}}{m_{00}} - x \tilde{A}_{R}^{2}, \frac{m_{11}}{m_{00}} - x \tilde{A}_{R} y \tilde{A}_{R}, \frac{m_{20}}{m_{02}} - y \tilde{A}_{R}^{2} \rangle$
Signal	Mean	$\mu(\mathbf{k}) = \sum_{i=0}^{\max i} i p_i(\mathbf{k})$
	Median	$v_{50}(k)$
	Energy	$E(\mathbf{k}) = \sum_{i=0}^{\max} i^2 p_i(\mathbf{k})$
	Variance	$\sigma^2(\mathbf{k}) = E^2(\mathbf{k}) - \mu^2(\mathbf{k})$
	Standard deviation	$\sigma({f k})=\sqrt{\sigma^2({f k})}$
	Dynamic range	$DR(k) = argmax_{\forall (x,y) \in k} i_{x,y} - argmin_{\forall (x,y) \in k} i_{x,y}$
	z-mean	$\overline{Z}(k) = rac{\mu(k)}{\sigma(k)}$
	Entropy	$H(\mathbf{k}) = \sum_{i=0}^{\max i} p_i(\mathbf{k}) \log p_i(\mathbf{k})$
	Skewness	$\gamma(\mathbf{k}) = \sum_{i=0}^{ ext{maxi}} p_i(\mathbf{k}) \Big(rac{i-\mu(\mathbf{k})}{\sigma(\mathbf{k})} \Big)^3$
	Kurtosis	$eta(\mathbf{k}) = \sum_{i=0}^{ ext{maxi}} p_i(\mathbf{k}) \Big(rac{i-\mu(\mathbf{k})}{\sigma(\mathbf{k})} \Big)^4 - 3$
	z-Range	$\mathrm{z}_{\mathrm{DR}}(\mathrm{k}) = rac{\mathrm{DR}(\mathrm{k})}{\sigma(\mathrm{k})}$
	² Fraction $<\sigma$	$p_{i < \sigma}(k) = \langle \sum_{i=0}^{v_{2\sigma}(k)} p_i(k), \sum_{i=0}^{v_{3\sigma}(k)} p_i(k) angle$
	² Fraction $>\sigma$	$p_{i < \sigma}(\mathtt{k}) = \langle \sum_{i = v_{2\sigma}(\mathtt{k})}^{ ext{maxi}} p_i(\mathtt{k}), \sum_{i = v_{3\sigma}(\mathtt{k})}^{ ext{maxi}} p_i(\mathtt{k}) angle$
	¹⁰ Percentile	$\upsilon_n(k):n=\langle 0.01, 0.1, a, e, 10, 25, 75, 90, 95, 99, 99.9, 99.99\rangle$
	Trimmed mean	$\mu_t(\mathbf{k}) = \sum_{i=\upsilon_5(\mathbf{k})}^{\upsilon_{95}(\mathbf{k})} ip_i(\mathbf{k})$
	Trimmed σ	$\sigma_{t}(\mathbf{k}) = \left[\sum_{i=\upsilon_{5}(\mathbf{k})}^{\upsilon_{95}(\mathbf{k})} (i - \mu_{t}(\mathbf{k}))^{2} p_{i}(\mathbf{k})\right]^{1/2}$
	Trimmed z-mean	$\overline{z}_t(\mathbf{k}) = rac{\mu_t(\mathbf{k})}{\sigma_t(\mathbf{k})}$
	Total signal	$M_{0,0} = \sum_{\forall (x,y) \in k} i_{x,y}$
	² Signal centroid	$q\tilde{A}_{S}(\textbf{k})=\langle x\tilde{A}_{S}(\textbf{k})=\frac{M_{10}}{M_{00}},y\tilde{A}_{S}(\textbf{k})=\frac{M_{01}}{M_{00}}\rangle$
	² Signal scatter	$S_{s}(k) = \langle \frac{M_{20}}{M_{00}} - x\tilde{A}_{S}^{2}, \frac{M_{11}}{M_{00}} - x\tilde{A}_{S}y\tilde{A}_{S}, \frac{M_{20}}{M_{02}} - y\tilde{A}_{S}^{2} \rangle$
	Signal surface	$A_{S} = \varDelta_{xy} \Big(\varDelta_{xy}^{2} + 4 \big(i_{x,y} - q \tilde{A}_{S}(k)\big)^{2}\Big)^{1/2}$

Numbers in superscript indicate the times a feature was measured, those without a superscript were measured once; $a_{x,y}$ is the unit area of a pixel; $d(e_i, e_{i+1})$ is the Euclidean distance between the ith and the ith + 1 neighboring edge points found in the set of edge points $\epsilon(k)$; L_q is the length of the bounding boxing the q axis; $m_{i,j}$ $M_{i,j}$ and the moment functions of the shape and the signal of k, respectively; $i_{x,y}$ is the intensity of the pixel at the x, y coordinates and $p_i(k)$ is the relative frequency of the ith intensity; $v_n(k)$ is the intensity of the pixel located at the nth% position of the ordered intensities of k; and $\Delta_{x,y}$ is the image size.

correlated features (Pearson correlation larger than 0.9), one of
such features was removed. Then, the feature selection procedure
was performed using a 10-fold cross-validation repeated 20 times.
This was done to avoid bias towards a specific data set partition.
False discovery rate was set to 0.025 to avoid non-statistical
significant features to be incorporated into the models.

³⁴⁵ **3. Results**

In order to have a full spectrum of the performance for theproposed methodology, accuracy, area under the receiver

operator characteristic (ROC) curve (AUC), sensitivity, and diagnostic odds ratio (dOR) were computed at different specificities (best, 0.5, 0.8, 0.9). Tables 3 and 4 show the results for the proposed methodology, and Figs. 4 and 5 show the ROC curve for the proposed methodology, for the BCDR and the DDSM data sets, respectively. All the results shown were computed using the ensembled prediction of the test, the one taking into account the results from the 20 iterations of the feature selection procedure.

The model selection strategy yielded reproducible models of healthy vs. non-healthy subjects with an AUC of 0.738 for the BCDR data set. An ODDS ratio of 23.10 was achieved along 357

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Table 2 – Distribution of mammograms.				
Subset	Healthy	Non-healthy	Total	
DDSM-Lumisys	32	56	88	
BCDR	23	41	64	
Total	55	97	152	

Table 3 – Healthy vs. non-healthy. Final model performance in the BCDR data set.					
Model	Accuracy	AUC	Sensitivity	Specificity	dOR
BSWIMS					
Best	0.672	0.738	0.512	0.957	23.100
specificity@0.5	0.586	0.738	0.634	0.500	1.733
specificity@0.8	0.647	0.738	0.561	0.800	5.111
specificity@0.9	0.667	0.738	0.537	0.900	10.421
KNN					
Best	0.563	0.683	0.366	0.913	6.058
specificity@0.5	0.662	0.683	0.753	0.500	3.049
specificity@0.8	0.569	0.683	0.440	0.800	3.141
specificity@0.9	0.563	0.683	0.374	0.900	5.386
LASSO					
Best	0.688	0.655	0.707	0.652	4.531
specificity@0.5	0.633	0.655	0.707	0.500	2.417
specificity@0.8	0.538	0.655	0.390	0.800	2.560
specificity@0.9	0.511	0.655	0.293	0.900	3.724

Table 4 – Healthy vs. non-healthy. Final model performance in the DDSM data set.					
Model	Accuracy	AUC	Sensitivity	Specificity	dOR
BSWIMS					
Best	0.750	0.767	0.750	0.750	9.000
specificity@0.5	0.682	0.767	0.786	0.500	3.667
specificity@0.8	0.689	0.767	0.625	0.800	6.667
specificity@0.9	0.634	0.767	0.482	0.900	8.379
KNN					
Best	0.693	0.758	0.589	0.875	10.043
specificity@0.5	0.698	0.758	0.811	0.500	4.297
specificity@0.8	0.686	0.758	0.621	0.800	6.541
specificity@0.9	0.580	0.758	0.396	0.900	5.911
LASSO					
Best	0.773	0.838	0.696	0.906	22.176
specificity@0.5	0.750	0.838	0.893	0.500	8.333
specificity@0.8	0.734	0.838	0.696	0.800	9.176
specificity@0.9	0.770	0.838	0.696	0.900	20.647

with a sensitivity of 0.512 and a specificity of 0.957. The bilateral model achieved a high specificity, making the Bilateral model highly suitable to detect the abnormalities. Classic KNN and LASSO feature selection methodologies achieved similar AUC results, nevertheless with a ODDS ratio of only 6.058 and 4.531 respectively.

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The ROC curve analysis for the BCDR data set is shown in Fig. 4, as we can see the ensemble prediction of the three feature selection algorithms have a similar performance with AUC ranging from 0.738, 0.683, 0.655 for B:SWiMS, KNN, and LASSO respectively. As we can see the use of patient features yields to reproducible models that can be used to triage the detection of abnormalities related to breast cancer.

On the other hand, the model selection B:SWiMS strategy 374 when used on the healthy vs. Other abnormalities in the DDSM 375 data set achieved an ensemble test AUC of 0.767. An ODDS 376 ratio of 9.00 was achieved along with a sensitivity of 0.750 and 377 a specificity of 0.750. as in the previous data set, the KNN and LASSO feature selection methodologies achieved similar AUC results, here, the ODDS ratio increased to a 10.043 and 22.176 respectively. The ROC curve analysis for the DDSM data set is shown in Fig. 4, the ensemble prediction of the three feature 382 selection algorithms have a similar performance with AUC 383 ranging from 0.767, 0.758 and 0.838 for B:SWiMS, KNN, and 384 LASSO respectively. As we can see the use of patient features 385 yields to reproducible models that can be used to triage the 386 detection of abnormalities related to breast cancer. 387

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Fig. 4 - ROC curves for the healthy vs. non-healthy classification in the BCDR data set.



Fig. 5 – ROC curves for the healthy vs. non-healthy classification in the DDSM data set.

4. Discussion

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Despite working with two different sets of images, one digital
and one analog, the proposed registration methodology was
able to successfully align the contralateral images. Once the
images were aligned, the bilateral image subtraction generated an asymmetry image, which was enhanced with four

different filters. Then, 880 subject-specific features were extracted. The creation of new features by merging the CC and MLO views helped to eliminate the dependency on view. The model selection strategy yielded reproducible models of healthy vs. non-healthy subjects for the BCDR and DDSM data sets. The bilateral approach model achieved a high specificity, making the Bilateral model highly suitable to detect any abnormalities and may be used to triage the detection of abnormalities related to breast cancer.

One key feature over previous approaches [33,48,49] is that they only try to detect breast cancer, i.e. only malignant cancer lesion, while our approach combine the benign and malign abnormalities into one category, that imply, the detection of the abnormality from the healthy ones regarding the type of abnormality i.e. (calcification, masses, architectural distortion, etc.) effectively making it a more complex problem, yet, obtaining great results. One of the main reason to combine said lesions, is that if leaved untreated benign abnormalities, they may evolve into malign lesions. The proposed methodology is fully automated, there is no need for human intervention as other approaches [50]. The proposed CADx system targets develop countries where the access to medical care is limited, and there is a deficit of trained radiologists, therefore a tool that successfully ranks the subjects according to the changes of having breast cancer related abnormalities may reduce the mortality rate. Moreover the models created using the patient features use subjects features rather than side specific mammograms as in other approaches. Even with different feature selection algorithms, LASSO, KNN, and B: SWIMS the performance was similar. This similar performance suggests that the proposed methodology is not specific to a particular feature selection algorithm. Moreover the achieve ODDS ratio of the presented model suggest a high association.

algorithm. Moreover the ed model suggest a high ection: A CADx approach. 394

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Table 5 – Similar approaches comparison.				
Author	Asymmetry approach	Туре	Performance	
Rodriguez-Rojas et al. [51]	Bilateral asymmetry used to classify low/high risk mammograms (bi-rads based) – genetic algorithm as feature selection	Feature-based	AUC = 0.88	
Martí et al. [49]	Use only MLO mammograms to classify abnormal/normal cases, bilateral feature-based, random forest-LOOCV	Temporal registration based	AUC = 0.76	
Zheng et al. [26]	Bilateral density asymmetry to classify high risk patients, temporal study	No registration	AUC = 0.761	
Wang et al. [28]	Feature-based bilateral asymmetry to classify low/high risk mammograms, ANN, no registration	Feature-based	AUC = 0.75	
Tan et al. [52]	Near-term breast cancer prediction, using feature based asymmetry SVM	Feature-based	AUC = 0.72	
Yin et al. [50] Our approach	Detection of masses, bilateral subtraction Detection of any type of abnormalities (MC, masses, etc.), bilateral subtraction	Manual registration Automated registration	A 95 % TP with a 3FP × image Two independent datasets with AUC of 0.738 and 0.767 respectively.	

428 In Table 5 a comparison against similar approaches is 429 presented, the authors acknowledge that there are several 430 approaches in the field of breast cancer detection, nevertheless, only approaches that incorporate some type of bilateral 431 analysis were included. In Table 5 we can see, that most of 432 the approaches does not incorporate any sort of alignment 433 prior the comparison, only Yin et al. [50] incorporate manual 434 bilateral registration, while Martí et al. [49] indeed includes 435 automatic registration but is limited to only temporal 436 registration. All other approaches [51,26,27,52] are feature-437 based only. The presented performance is similar to those 438 that incorporate any asymmetry analysis, nevertheless, our 439 approach was validated in two independent and different 440 type of mammograms (digital and film), even further, those 441 datasets included different ethnicities, while the others were 442 tested only on a single dataset. When comparing our 443 444 approach with others, we can notice that all others only 445 try to detect breast cancer (i.e. only malignant cancer 446 lesions), while our approach combine the benign and malign 447 abnormalities into one category, that implies, the detection 448 of the abnormality from the healthy ones regarding the type of abnormality, i.e. (calcification, masses, architectural 449 450 distortion, etc.). Even further, our approach fusions the features from the CC and MLO views, successfully creating a 451 452 score for each patients while others only output a score for a single mammogram, this approach may output false 453 454 negatives in some cases where the same breast (i.e. left) may score positive for CC and it may also score negative for 455 the same MLO view, while in our fusion approach the 456 features are patient-based and not bias towards a specific 457 view as others. 458

This research was performed using a Quad core (8 threads) 459 Xeon processor at 3.0 GHz, 16 GB of RAM, the average time for 460 461 the image processing stage was 9-11 minutes by each subject, 462 on the feature selection, FRESA.CAD use the FPR to reduce the 463 number of features in each selection stage, the algorithm have 464 a complexity of O(ndk), where n is the cardinality of the 465 training set, d is the dimension of each sample and k is the 466 model size. the average computational time was on average 20 minutes, nevertheless, FRESA.CAD can work on multiple cores 467 468 at the same time reducing the time according the resources

available. The FRESA.CAD time may be somehow long, but the training phase needs to be carryout once.

The proposed methodology exhibits some limitations, among them, there is the necessity of the CC and MLO from the left and right mammograms, this may leave out subjects that undergo only to a specific side mammogram, or women that went under surgical mastectomy and therefore the bilateral analysis can not be performed. Other limitation reside in subjects with breast implants, that due the high radioluminiscent of the implant, it may lead to unrealistic bilateral registration of the breasts, therefore, limiting the use to women without breast implants.

5. Conclusions

The presented CADx methodology yielded to the creation of patient features that fusion the information of contralateral asymmetry and the different views into single features. The methodology was validated in two independent data sets using both analog and digital mammograms, and different type of scanners. The achieved results shown that the methodology could classify healthy subjects from any other type of cancer or benign abnormality, to our knowledge it is the first approach that works with any other type of abnormality. The proposed methodology yielded reproducible and similar results even with different model selection strategies. The models have the potential to be used to queue cases with a high chance of malignant findings, effectively reducing the radiologist workload. Such models have the practical use of triaging mammograms in developing countries where there is a deficiency of expert readers.

Future work will focus on validating the methodology on clinical scenarios and the implications of translating this methodology to health systems.

Conflict of interest

The authors declare that there is no conflict of interest regarding the publication of this manuscript.

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508 REFERENCES

- 509 [1] DeSantis C, Ma J, Bryan L, Jemal A. Breast cancer statistics,
 510 2013. CA: Cancer J Clin 2014;64:52–62.
 - [2] Miller AB, Wall C, Baines CJ, Sun P, To T, Narod SA. Twenty five year follow-up for breast cancer incidence and mortality of the Canadian National Breast Screening Study: randomised screening trial. BMJ 2014;348.
 - [3] Løberg M, Lousdal ML, Bretthauer M, Kalager M. Benefits and harms of mammography screening. Breast Cancer Res 2015;17:63.
 - [4] Rangayyan RM, Ayres FJ, Leo Desautels JE. A review of computer-aided diagnosis of breast cancer: toward the detection of subtle signs. J Franklin Inst 2007;344:312–48.
- [5] Bleyer A, Welch HG. Effect of three decades of screening mammography on breast-cancer incidence. N Engl J Med 2012;367:1998–2005.
- [6] Ng EY-K, Fok S-C. A framework for early discovery of breast tumor using thermography with artificial neural network.
 Breast J 2003;9:341–3.
- 527 [7] Ng E, Kee E, Acharya UR. Advanced technique in breast 528 thermography analysis. 27th Annual International 529 Conference of the Engineering in Medicine and Biology 530 Society, IEEE-EMBS 2005. IEEE; 2005. p. 710–3.
- [8] Skaane P, Bandos AI, Gullien R, Eben EB, Ekseth U,
 Haakenaasen U, et al. Prospective trial comparing full-field
 digital mammography (ffdm) versus combined ffdm and
 tomosynthesis in a population-based screening programme
 using independent double reading with arbitration. Eur
 Radiol 2013;23:2061–71.
- [9] Houssami N, Bernardi D, Pellegrini M, Valentini M, Fantò C,
 Ostillio L, et al. Breast cancer detection using single-reading
 of breast tomosynthesis (3d-mammography) compared to
 double-reading of 2d-mammography: evidence from a
 population-based trial. Cancer Epidemiol 2017;47:94–9.
 - [10] Doi K. Computer-aided diagnosis in medical imaging: historical review, current status and future potential. Comput Med Imaging Graph 2007;31:198–211.
- 545 [11] Lee H, Chen Y-PP. Image based computer aided diagnosis
 546 system for cancer detection. Expert Syst Appl 2015;42:
 547 5356–65.
 - [12] Lo C-M, Chang R, Huang C, Moon W. Computer-aided diagnosis of breast tumors using textures from intensity transformed sonographic images. 1st Global Conference on Biomedical Engineering & 9th Asian-Pacific Conference on Medical and Biological Engineering. Springer; 2015. p. 124–7.
 - [13] Ganesan K, Acharya UR, Chua CK, Min LC, Abraham KT, Ng K-H. Computer-aided breast cancer detection using mammograms: a review. IEEE Rev Biomed Eng 2013;6:77–98.
- [14] Tang J, Rangayyan RM, Xu J, El Naqa I, Yang Y. Computeraided detection and diagnosis of breast cancer with
 mammography: recent advances. IEEE Trans Inform
 Technol Biomedon 2009;13:236–51.
- [15] Oliver A, Freixenet J, Marti J, Pérez E, Pont J, Denton ERE,
 et al. A review of automatic mass detection and
 segmentation in mammographic images. Med Image Anal
 2010;14:87–110.
- [16] Dhungel N, Carneiro G, Bradley AP. A deep learning
 approach for the analysis of masses in mammograms with
 minimal user intervention. Med Image Anal 2017;37:114–28.

- [17] Baker JA, Rosen EL, Lo JY, Gimenez EI, Walsh R, Soo MS. Computer-aided detection (CAD) in screening mammography: sensitivity of commercial CAD systems for detecting architectural distortion. Am J Roentgenol 2003;181:1083–8.
- [18] Eadie LH, Taylor P, Gibson AP. A systematic review of computer-assisted diagnosis in diagnostic cancer imaging. Eur J Radiol 2012;81:e70–6.
- [19] Dromain C, Boyer B, Ferre R, Canale S, Delaloge S, Balleyguier C. Computed-aided diagnosis (CAD) in the detection of breast cancer. Eur J Radiol 2013;82:417–23.
- [20] Kozegar E, Soryani M, Minaei B, Domingues I. Assessment of a novel mass detection algorithm in mammograms. J Cancer Res Therap 2013;9:592.
- [21] de Sampaio WB, Silva AC, de Paiva AC, Gattass M. Detection of masses in mammograms with adaption to breast density using genetic algorithm, phylogenetic trees, lbp and svm. Expert Syst Appl 2015;42:8911–28.
- [22] Doi K. Current status and future potential of computeraided diagnosis in medical imaging. Br J Radiol 2014.
- [23] Miranda GHB, Felipe JC. Computer-aided diagnosis system based on fuzzy logic for breast cancer categorization. Comput Biol Med 2015;64:334–46.
- [24] Dheeba J, Singh NA. Computer aided intelligent breast cancer detection: second opinion for radiologists – a prospective study. Computational Intelligence Applications in Modeling and Control. Springer; 2015. p. 397–430.
- [25] Raghavendra U, Acharya UR, Fujita H, Gudigar A, Tan JH, Chokkadi S. Application of gabor wavelet and locality sensitive discriminant analysis for automated identification of breast cancer using digitized mammogram images. Appl Soft Comput 2016;46:151–61.
- [26] Zheng B, Sumkin JH, Zuley ML, Wang X, Klym AH, Gur D. Bilateral mammographic density asymmetry and breast cancer risk: a preliminary assessment. Eur J Radiol 2012;81:3222–8.
- [27] Wang X, Lederman D, Tan J, Wang XH, Zheng B. Computerized prediction of risk for developing breast cancer based on bilateral mammographic breast tissue asymmetry. Med Eng Phys 2011;33:934–42.
- [28] Wang X, Lederman D, Tan J, Wang XH, Zheng B. Computerized detection of breast tissue asymmetry depicted on bilateral mammograms: a preliminary study of breast risk stratification. Acad Radiol 2010;17:1234–41.
- [29] Scutt D, Manning JT, Whitehouse GH, Leinster SJ, Massey CP. The relationship between breast asymmetry, breast size and the occurrence of breast cancer. Br J Radiol 1997;70:1017–21.
- [30] Suri JS, Rangayyan RM. Recent advances in breast imaging, mammography, and computer-aided diagnosis of breast cancer, volume 155. SPIE press; 2006.
- [31] Miller P, Astley SM. Detection of breast asymmetry using anatomical features. IS&T/SPIE's Symposium on Electronic Imaging: Science and Technology. International Society for Optics and Photonics; 1993. p. 433–42.
- [32] Miller P, Astley S. Automated detection of breast asymmetry using anatomical features. State of the Art in Digital Mammographic Image Analysis, Series in Machine Perception and Artificial Intelligence, vol. 9. 1994. pp. 247–61.
- [33] Ferrari RJ, Rangayyan RM, Desautels JEL, Borges RA, Frere AF. Automatic identification of the pectoral muscle in mammograms. IEEE Trans Med Imaging 2004;23:232–45.
- [34] Torrents-Barrena J, Puig D, Melendez J, Valls A. Computeraided diagnosis of breast cancer via gabor wavelet bank and binary-class svm in mammographic images. J Exp Theoret Artif Intell 2016;28:295–311.
- [35] Evans KK, Haygood TM, Cooper J, Culpan A-M, Wolfe JM. A half-second glimpse often lets radiologists identify breast

Please cite this article in press as: Celaya-Padilla JM, et al. Contralateral asymmetry for breast cancer detection: A CADx approach. Biocybern Biomed Eng (2017), https://doi.org/10.1016/j.bbe.2017.10.005

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Nonrigid multimodality image registration. Medical Imaging 2001. International Society for Optics and

2015:2015.

Biol 1995:40:857.

Photonics; 2001. p. 1609-20. [40] Rangayyan RM, Banik S, Desautels JEL. Computer-aided detection of architectural distortion in prior mammograms

cancer cases even when viewing the mammogram of the

opposite breast. Proc Natl Acad Sci USA 2016;113:10292-7.

Galvan-Tejada J. Treviño V. Tamez-Peña J. Bilateral image

subtraction and multivariate models for the automated

Goodsitt MM, et al. Computer-aided classification of

discriminant analysis in texture feature space. Phys Med

analysis, vol. 12. Springer Science & Business Media; 2013.

[39] Mattes D, Haynor DR, Vesselle H, Lewellyn TK, Eubank W.

mammographic masses and normal tissue: linear

[36] Celaya-Padilla J, Martinez-Torteya A, Rodriguez-Rojas J,

triaging of screening mammograms. BioMed Res Int

[37] Chan H-P, Wei D, Helvie MA, Sahiner B, Adler DD,

[38] Rosenfeld A. Multiresolution image processing and

of interval cancer. J Dig Imaging 2010;23:611-31. [41] Ibanez L, Schroeder W, Ng L, Cates J. The ITK software

guide. Kitware; 2003. [42] Ganesan K, Acharya UR, Chua KC, Min LC, Abraham KT. Pectoral muscle segmentation: a review. Comput Methods Programs Biomed 2013;110:48-57.

[43] Galván-Tejada CE, Zanella-Calzada LA, Galván-Tejada JI, Celaya-Padilla JM, Gamboa-Rosales H, Garza-Veloz I, et al. Multivariate feature selection of image descriptors data for breast cancer with computer-assisted diagnosis. Diagnostics 2017;7:9.

666 [44] Galván-Tejada CE, García-Vázquez JP, García-Ceja E, Carrasco-Jiménez JC, Brena RF. Evaluation of four classifiers 668

Biocybern Biomed Eng (2017), https://doi.org/10.1016/j.bbe.2017.10.005

as cost function for indoor location systems. Proc Comput Sci 2014:32:453-60.

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698

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700

701

702

- [45] Heath M, Bowyer K, Kopans D, Moore R, Kegelmeyer P. The digital database for screening mammography. Proceedings of the 5th International Workshop on Digital Mammography; 2000. p. 212-8.
- [46] López MAG, de Posada NG, Moura DC, Pollán RR, Valiente JMF, Ortega CS, et al. BCDR: a breast cancer digital repository. 15th International Conference on Experimental Mechanics; 2012.
- [47] Beasley TM, Erickson S, Allison DB. Rank-based inverse normal transformations are increasingly used, but are they merited? Behav Genet 2009;39:580-95.
- [48] Diez Y, Oliver A, Lladó Xavier, Freixenet J, Marti J, Vilanova JC, et al. Revisiting intensity-based image registration applied to mammography. IEEE Trans Inform Technol Biomed 2011;15:716-25.

[49] Martí R, Díez Y, Oliver A, Tortajada M, Zwiggelaar R, Lladó X.

Detecting abnormal mammographic cases in temporal

[50] Yin F, Giger ML, Doi K, Metz CE, Vyborny CJ, Schmidt RA.

mammograms: analysis of bilateral subtraction images.

[51] Rodriguez-Rojas J, Garza-Montemayor M, Trevino-Alvarado

V, Tamez-Pena JG. Predictive features of breast cancer on

Mexican screening mammography patients. SPIE Medical

term breast cancer risk based on bilateral mammographic

Imaging. International Society for Optics and Photonics;

[52] Tan M, Zheng B, Ramalingam P, Gur D. Prediction of near-

feature asymmetry. Acad Radiol 2013;20:1542-50.

Computerized detection of masses in digital

Springer; 2014. p. 612-9.

Med Phys 1991:18:955-63.

2013. p. 867023-9.

Please cite this article in press as: Celaya-Padilla JM, et al. Contralateral asymmetry for breast cancer detection: A CADx approach.

studies using image registration features. Breast Imaging.